

# exponent progression

$$x^n = \alpha$$

$$x^n - 2 = \beta$$

$$\alpha x^a = 4$$

$$\alpha x^a - 4 = \beta$$

$$4x^a x^b - \alpha = 2$$

$$\frac{x}{2x^a} - \beta = 1$$

$$4(\alpha x^n)^2 + (x^2)^n = 1$$

$$(2\sqrt{x})^\alpha - x^{\frac{\alpha}{n}} = \beta$$

$$\sqrt{x^2 - \alpha^2} = \alpha x$$

with terms

with coefficients

combined

adding exponents

subtracting exponents

expand/reverse brackets

include radicals

trick questions

# exponents with letters

$$x^n = \alpha$$

$$x^n + 4 = \beta$$

$$x^{-n} - n = \alpha$$

$$\alpha x^a = 4$$

$$\beta x^b - 4 = \alpha$$

$$\alpha x^a - 1 = \beta$$

$$\frac{\alpha^n - x^n}{4} + 2 = \alpha$$

$$\frac{4x^n - 4(x^n - \alpha)}{x^\alpha} + 2 = \beta$$

$$\frac{x^n - \alpha}{\alpha} + \beta = e(1-\pi)^n$$

$$\frac{x(1-x^2)}{2x} + \alpha x^2 = e$$

$$x^a x^2 + 2 = 4$$

$$\frac{x^n x^{-n}}{2} + 4x^a = \epsilon$$

$$\frac{x^a x^n x}{4 - \alpha} + \Gamma(\alpha - 1)^n = 2$$

$$\frac{x^m x}{x} + 2 = \epsilon$$

$$\frac{x^n(1-\alpha)}{\beta(1+\alpha)} + 2 = \epsilon$$

$$\frac{x^n x^2}{x} + 4 = \sum_{i=1}^n r_i^2$$



$$\frac{x^n}{x^m(1-\alpha)} + 4 = e$$

$$\frac{x^2(1-e)}{x^\alpha(1+e)} = m$$

$$(2x)^2 + x^2 = \alpha$$

$$[(\alpha - 1)x]^n - 4 = \epsilon$$

$$[\alpha x]^n - x^n = 18$$

$$[(\alpha - 1)x^2]^n - [2x^n]^2 = 8$$

$$\left[ \frac{\alpha x^2}{x^a} \right]^b = e$$

$$\sqrt{x^a} = 4$$

$$\left[ \frac{x^{\frac{1}{2}} \sqrt{x}}{x} \right]^2 - x = 0$$

$$\left[ \sqrt[3]{x^{\alpha}} x^{\frac{3}{\alpha}} \right]^2 + e = 8$$

$$\left[ 2 \sqrt[3]{x^\alpha} \right]^{\frac{3}{\alpha}} - x = 4$$

$$\sqrt{x^2 - \alpha^2} = \alpha x$$

$$(x^2 + 1)^{\frac{1}{2}} + 2 = e^n$$

$$\sqrt{(4-x)^2 + 4^2} = e + 1$$

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# exponents with letters

$$(x^n)^{\frac{1}{n}} = (\alpha)^{\frac{1}{n}}$$

$$x = \alpha^{\frac{1}{n}}$$

$$x^n + 4 = \beta$$

$$(x^n)^{\frac{1}{n}} = (\beta - 4)^{\frac{1}{n}}$$

$$x = [\beta - 4]^{\frac{1}{n}}$$

$$x^{-n} - n = \alpha$$

$$(x^{-n})^{\frac{1}{-n}} = (\alpha + n)^{\frac{1}{-n}}$$

$$x = (\alpha + n)^{-\frac{1}{n}} = \frac{1}{\sqrt[n]{\alpha + n}}$$

$$\frac{\alpha x^a}{\alpha} = \frac{4}{\alpha}$$

$$(x^a)^{\frac{1}{a}} = \left(\frac{4}{\alpha}\right)^{\frac{1}{a}}$$

$$x = \left(\frac{4}{\alpha}\right)^{\frac{1}{a}}$$

$$\beta x^b - 4^{+4} = \alpha^{+4}$$

$$\frac{\beta x^b}{\beta} = \frac{\alpha + 4}{\beta}$$

$$(x^b)^{\frac{1}{b}} = \left(\frac{\alpha + 4}{\beta}\right)^{\frac{1}{b}}$$

$$x = \left(\frac{\alpha + 4}{\beta}\right)^{\frac{1}{b}}$$

$$\alpha x^\alpha - 1^{+1} = \beta^{+1}$$

$$\frac{\alpha x^\alpha}{\alpha} = \frac{\beta + 1}{\alpha}$$

$$(x^\alpha)^{\frac{1}{\alpha}} = \left(\frac{\beta + 1}{\alpha}\right)^{\frac{1}{\alpha}}$$

$$x = \left(\frac{\beta + 1}{\alpha}\right)^{\frac{1}{\alpha}}$$

$$\frac{\alpha^n - x^n}{4} + 2^{\alpha} = \alpha^{\alpha}$$

$$4 \left( \frac{\alpha^n - x^n}{4} \right) = (\alpha - 2) 4$$

$$\alpha^n - x^n = 4(\alpha - 2)^{\alpha^n}$$

$$(-1)(-x^n) = (4(\alpha - 2) - \alpha^n)^{(-1)}$$

$$(x^n)^{\frac{1}{n}} = (\alpha^n - 4(\alpha - 2))^{\frac{1}{n}}$$

$$x = [\alpha^n - 4(\alpha - 2)]^{\frac{1}{n}}$$

$$\frac{4x^n - 4(x^n - \alpha)}{x^\alpha} + 2^{\alpha} = \beta^{\alpha}$$

$$x^\alpha \left( \frac{4x^n - 4x^n + 4\alpha}{x^\alpha} \right) = (\beta - 2) x^\alpha$$

$$4\alpha = (\beta - 2) x^\alpha$$

$$(x^\alpha)^{\frac{1}{\alpha}} = \left( \frac{4\alpha}{\beta - 2} \right)^{\frac{1}{\alpha}}$$

$$x = \left[ \frac{4\alpha}{\beta - 2} \right]^{\frac{1}{\alpha}}$$

$$\frac{x^n - \alpha}{\alpha} + \beta = e(1-\Gamma)^n$$

$$\alpha \left( \frac{x^n - \alpha}{\alpha} \right) = (e(1-\Gamma)^n - \beta) \alpha$$

$$x^n - \alpha = \alpha e(1-\Gamma)^n - \alpha \beta$$

$$(x^n)^{\frac{1}{n}} = (\alpha e(1-\Gamma)^n - \alpha \beta + \alpha)^{\frac{1}{n}}$$

$$x = [\alpha e(1-\Gamma)^n - \alpha \beta + \alpha]^{\frac{1}{n}}$$

$$2 \left( \frac{x(1-x^2)}{2x} + \alpha x^2 \right) = e \cdot 2$$

$$1 - x^2 + 2\alpha x^2 = 2e$$

$$(2\alpha x^2 - x^2) = 2e - 1$$

$$x^2(2\alpha - 1) = 2e - 1$$

$$(x^2)^{\frac{1}{2}} = \left( \frac{2e - 1}{2\alpha - 1} \right)^{\frac{1}{2}}$$

$$x = \pm \left( \frac{2e - 1}{2\alpha - 1} \right)^{\frac{1}{2}}$$

$$x^{a+2} + 2 = 4$$

$$(x^{a+2})^{\frac{1}{2+a}} = (2)^{\frac{1}{2+a}}$$

$$x = 2^{\frac{1}{2+a}}$$

$$\frac{x^n x^{-n}}{2} + 4x^\alpha = e$$

$$2 \left( \frac{x^0}{2} + 4x^\alpha \right) = (e) 2$$

$$1 + 8x^\alpha = 2e$$

$$8x^\alpha = 2e - 1$$

$$(x^\alpha)^{\frac{1}{\alpha}} = \left( \frac{2e - 1}{8} \right)^{\frac{1}{\alpha}}$$

$$x = \left( \frac{2e - 1}{8} \right)^{\frac{1}{\alpha}}$$

$$\frac{x^{\overbrace{a+n}^{=a+n+1}}}{4-\alpha} + \Gamma(\alpha-1)^n = 2^{-\Gamma(\alpha-1)^n}$$

$$(4-\alpha) \left( \frac{x^{a+n+1}}{4-\alpha} \right) = \left( 2 - \Gamma(\alpha-1)^n \right) (4-\alpha)$$

$$\left( x^{a+n+1} \right)^{\frac{1}{a+n+1}} = \left( \left( 2 - \Gamma(\alpha-1)^n \right) (4-\alpha) \right)^{\frac{1}{a+n+1}}$$

$$x = \left[ \left( 2 - \Gamma(\alpha-1)^n \right) (4-\alpha) \right]^{\frac{1}{a+n+1}}$$

$$\frac{x^m x}{x} + 2^{-2} = \epsilon^{-2}$$

$$x^{\overbrace{m}^{=m}} x^{-1} = \epsilon - 2$$

$$\left( x^m \right)^{\frac{1}{m}} = \left( \epsilon - 2 \right)^{\frac{1}{m}}$$

$$x = \left( \epsilon - 2 \right)^{\frac{1}{m}}$$



$$\frac{x^n(1-\alpha)}{\beta(1+\alpha)} + 2^{\text{red}} = \epsilon^{\text{red}}$$

$$\beta(1+\alpha) \left( \frac{x^n(1-\alpha)}{\beta(1+\alpha)} \right) = (\epsilon - 2) \beta(1+\alpha)$$

$$x^n(1-\alpha) = (\epsilon - 2) \beta(1+\alpha)$$

$$(x^n)^{\frac{1}{n}} = \left( \frac{\beta(\epsilon - 2)(1+\alpha)}{1-\alpha} \right)^{\frac{1}{n}}$$

$$x = \left[ \beta \frac{(\epsilon - 2)(1+\alpha)}{1-\alpha} \right]^{\frac{1}{n}}$$

$$\frac{x^{\overset{=n+1}{n}} x^2}{x} + 4^{\text{red}} = \sum_{i=1}^n r_i^2^{\text{red}}$$

$$(x^{n+1})^{\frac{1}{n+1}} = \left( \sum_{i=1}^n r_i^2 - 4 \right)^{\frac{1}{n+1}}$$

$$x = \left[ \sum_{i=1}^n r_i^2 - 4 \right]^{\frac{1}{n+1}}$$

$$\frac{x^n}{x^m(1-\alpha)} + 4 = \epsilon$$

$$(1-\alpha) \left( \frac{x^n}{x^m(1-\alpha)} \right) = (\epsilon - 4)(1-\alpha)$$

$$\left( \frac{x^{-m}}{x^{-m}} \right) \frac{x^n}{x^m} = (\epsilon - 4)(1-\alpha)$$

$$\left( x^{n-m} \right)^{\frac{1}{n-m}} = \left( (\epsilon - 4)(1-\alpha) \right)^{\frac{1}{n-m}}$$

$$x = \left[ (\epsilon - 4)(1-\alpha) \right]^{\frac{1}{n-m}}$$

$$\left( \frac{x^{-\alpha}}{x^{-\alpha}} \right) \frac{x^2(1-\epsilon)}{x^\alpha(1+\epsilon)} = w$$

$$\left( \frac{1+\epsilon}{1-\epsilon} \right) \left( \frac{x^{2-\alpha}(1-\epsilon)}{1+\epsilon} \right) = w \left( \frac{1+\epsilon}{1-\epsilon} \right)$$

$$\left( x^{2-\alpha} \right)^{\frac{1}{2-\alpha}} = \left( \frac{w(1+\epsilon)}{1-\epsilon} \right)^{\frac{1}{2-\alpha}}$$

$$x = \left[ w \frac{1+\epsilon}{1-\epsilon} \right]^{\frac{1}{2-\alpha}}$$



$$(2x)^2 + x^2 = \alpha$$

$$4x^2 + x^2 = \alpha$$

$$\frac{5x^2}{5} = \frac{\alpha}{5}$$

$$(x^2)^{\frac{1}{2}} = \left(\frac{\alpha}{5}\right)^{\frac{1}{2}}$$

$$x = \left(\frac{\alpha}{5}\right)^{\frac{1}{2}}$$

$$[(\alpha-1)x]^n - 4 = \epsilon$$

$$\left[(\alpha-1)x\right]^n = (\epsilon+4)^{\frac{1}{n}}$$

$$(\alpha-1)x = (\epsilon+4)^{\frac{1}{n}}$$

$$x = \frac{(\epsilon+4)^{\frac{1}{n}}}{(\alpha-1)}$$

$$[\alpha x]^n - x^n = 18$$

$$\alpha^n x^n - x^n = 18$$

$$x^n(\alpha^n - 1) = 18$$

$$(x^n)^{\frac{1}{n}} = \left( \frac{18}{\alpha^n - 1} \right)^{\frac{1}{n}}$$

$$x = \left[ \frac{18}{\alpha^n - 1} \right]^{\frac{1}{n}}$$

$$[(\alpha - 1)x^2]^n - [2x^n]^2 = 8$$

$$(\alpha - 1)^n x^{2n} - 4x^{2n} = 8$$

$$x^{2n} [(\alpha - 1)^n - 4] = 8$$

$$(x^{2n})^{\frac{1}{2n}} = \left( \frac{8}{[(\alpha - 1)^n - 4]} \right)^{\frac{1}{2n}}$$

$$x = \left( \frac{8}{(\alpha - 1)^n - 4} \right)^{\frac{1}{2n}}$$

$$\left( \left[ \frac{\alpha x^2}{x^a} \right]^b \right)^{\frac{1}{b}} = (e)^{\frac{1}{b}}$$

$$\alpha x^{2-a} = e^{\frac{1}{b}}$$

$$\left( x^{2-a} \right)^{\frac{1}{2-a}} = \left( \frac{e^{\frac{1}{b}}}{\alpha} \right)^{\frac{1}{2-a}}$$

$$x = \left[ \frac{e^{\frac{1}{b}}}{\alpha} \right]^{\frac{1}{2-a}}$$

$$\sqrt{x^a} = 4$$

$$(x^a)^{\frac{1}{2}} = 4$$

$$\left( x^{\frac{a}{2}} \right)^{\frac{2}{a}} = (4)^{\frac{2}{a}}$$

$$x = 4^{\frac{2}{a}} = 16^{\frac{1}{a}}$$

$$\left[ \frac{x^{\frac{1}{2}} \sqrt{x}}{x} \right]^2 - x = 0$$

$$\left[ x^{\frac{1}{2}} x^{\frac{1}{2}} x^{-1} \right]^2 - x = 0$$

$$\left[ x^0 \right]^2 - x = 0$$

$$\left[ 1 \right]^2 - x = 0$$

$$\boxed{x = 1}$$

$$\left[ \sqrt[3]{x^\alpha} x^{\frac{3}{\alpha}} \right]^2 + \epsilon = 8$$

$$\left[ x^{\frac{\alpha}{3}} x^{\frac{3}{\alpha}} \right]^2 = 8 - \epsilon$$

$$x^{\frac{\alpha}{3} + \frac{3}{\alpha}} = (8 - \epsilon)^{\frac{1}{2}}$$

$$\boxed{x = \left[ 8 - \epsilon \right]^{\frac{1}{2(\frac{\alpha}{3} + \frac{3}{\alpha})}}}$$

$$\left[ 2 \sqrt[3]{x^{\alpha}} \right]^{\frac{3}{\alpha}} - x = 4$$

$$\left[ 2 x^{\frac{\alpha}{3}} \right]^{\frac{3}{\alpha}} - x = 4$$

$$2^{\frac{3}{\alpha}} x - x = 4$$

$$x(2^{\frac{3}{\alpha}} - 1) = 4$$

$$x = \frac{4}{8^{\frac{1}{\alpha}} - 1}$$

$$\sqrt{x^2 - \alpha^2} = \alpha x$$

$$(x^2 - \alpha^2)^{\frac{1}{2}} = \alpha x$$

$$x^2 - \alpha^2 = (\alpha x)^2$$

$$x^2 - \alpha^2 = \alpha^2 x^2$$

$$x^2 - \alpha^2 x^2 = \alpha^2$$

$$x^2(1 - \alpha^2) = \alpha^2$$

$$(x^2)^{\frac{1}{2}} = \left( \frac{\alpha^2}{1 - \alpha^2} \right)^{\frac{1}{2}}$$

$$x = \left( \frac{\alpha^2}{1 - \alpha^2} \right)^{\frac{1}{2}}$$

$$x = \frac{\alpha}{(1 - \alpha^2)^{\frac{1}{2}}} = \frac{\alpha}{\sqrt{1 - \alpha^2}}$$

$$(x^2 + 1)^{\frac{1}{2}} + 2 = e^{n-2}$$

$$\left((x^2 + 1)^{\frac{1}{2}}\right)^2 = (e^n - 2)^2$$

$$x^2 + 1 = (e^n - 2)^2$$

$$(x^2)^{\frac{1}{2}} = ((e^n - 2)^2 - 1)^{\frac{1}{2}}$$

$$x = \pm \left([e^n - 2]^2 - 1\right)^{\frac{1}{2}}$$

$$\sqrt{(4-x)^2 + 4^2} = e + 1$$

$$\left[(4-x)^2 + 4^2\right]^{\frac{1}{2}} = (e + 1)^2$$

$$(4-x)^2 + 16 = (e + 1)^2$$

$$(4-x)^2 = (e + 1)^2 - 16$$

$$4 - x = \left[(e + 1)^2 - 16\right]^{\frac{1}{2}}$$

$$x = 4 - \left[(e + 1)^2 - 16\right]^{\frac{1}{2}}$$